

Probable Optimization of Reactive Power in distribution systems, in presence of distributed generation sources conjugated to network and islanding

Qolamreza Nematollahi, Esmail Khalilzadeh, Mohammadreza Aghaei,
Mojtaba Borhani

12 Azad University Branch of Marvdasht
34 Azerbaijan Power Consulting Engineering Company

Abstract: *In this article Probable Optimization of Reactive Power in distribution systems, in presence of distributed generation sources conjugated to network and islanding has been presented. For probable assessment of success operation of micro grids based on active and reactive power quality and consideration of voltage limitation, a systematic and optimized strategy for optimum placement of generation resources has been presented. The problem has been solved by the taboo search optimization algorithm and consideration of two objective function. First objective function is the annual energy loss and second one is a novel index in micro grid succession assessment based on active and reactive power quality and voltage limitations. Then the reactive optimum power is designed for reduction of annual energy loss of systems conjugated to network. By a case study in this article it will be shown that placement location and the amount of distributed generation resources have the considerable effect on micro grids operations.*

Keywords: *Energy loss, micro grid operation, optimum placement, reactive power designing, taboo search.*

I. Introduction

Distributed Reactive Sources (DRS) used in distribution networks for some reasons such as decreasing the energy loss, improving the voltage profile, rectifying the power coefficient and increasing the Capacitance of system. Optimum designing of reactive power or especially the optimum locating of capacitor in distribution networks, performed many times by the power engineers for different aims such as peak power, energy loss, cost decreasing and improving the distribution network reliability (Etemadi and Fotuhi-Firuzabad 2008). Different methods suggested in this domain, from the previous analytical methods (Mekhamer et al. 2002) to innovative and intelligent methods (Dadkhah and Venkatesh 2012). Changing the distribution system structure because of the micro-grids entrance, probable nature of added distributed productions and their ability in reactive power providing, caused to understand the necessity of designing and new strategy in extraction for current distribution systems. In present study, optimum locating and measuring of old reactive sources will be reviewed, considering the novel system's circumstances. For this aim, the problems of reactive power designing in distribution systems will be formulated, considering the different sides of modern distribution systems. These properties for reactive power designing have not been stated by Etemadi and Fotuhi-Firuzabad 2008; Mekhamer et al. 2002; Dadkhah and Venkatesh 2012 in literature. Two objective functions considered in this article. First aim is minimizing the annual energy loss in link to the network condition and second aim is maximizing the novel defined index for success performance in islanding situation at feeding-losing condition. The main part of this article is about the researches of optimized reactive power designing in modern distribution systems.

Problem Mathematical Explanation

In this section, the objective function equations will be explained. In this article, the DRS's reactive power presented in general form but they can be considered as the capacitor banks that are so affordable. In situations that distributed productions should be used along with power electronic convertors or in situation that capacitors are changeable the same equations, algorithms and analyzes used. Only differences is that the DRS capacities for all load-production states will be variable. Finally, the maximum calculated capacity of DRSs in each situation assumed the optimum capacity of it.

A. Energy Losses

It is possible to minimize the annual energy losses via the DRSs location optimizing in distribution system. Minimizing the energy losses can be an important goal for network designers. In this article, some cases such as variable characteristic of distributed generations and load profile will be considered for minimizing the annual energy losses. Objective function defined as below:

$$F_1 = \text{Annual losses of energy} \quad (1)$$

$$= \sum_{n=1}^N P_{Loss_n} \times \rho_n \times h_n$$

Where N is the number of states in a year, P_{Loss_n} is the system losses for a distinct time from a year, ρ_n is the related probability state and h_n is a time part of related state that is considered one hour here. Via the optimum locating and measuring of DRSSs, it is possible to reduce the total energy losses.

B. Micro Grid Success Index

Micro grids can be used in islanding form to provide critical loads at outage of main feeding source and improve the distribution system reliability. One circumstance for success performance in islanding state is as below:

$$P_{DG} \geq P_{Load} + P_{Loss} \quad (2)$$

Where P_{DG} is the generated power by the micro grid DGs, P_{load} is the load power in island and P_{loss} is the power losses of the island and assumed that is 5% of current load (Jain, Singh, and Srivastava 2013). It is assumed that biomass distributed generation units are programmable and is the second circumstance of success operation of micro grid (Pilo, Pisano, and Soma 2011).

$$P_{BM} \geq 0.6 \times P_{DG} \quad (3)$$

Where P_{BM} is the generated power by the Biomass DGs in micro grid. Equation 2 and 3 are the necessary circumstances for the success performance of micro grid. There are 365*3456 state with different probability for each state. Calculating the defined index for each micro grid, each state calculate separately and zero or one given to each one.

$$\rho_{\mu Gi} = \left\{ \begin{array}{l} 1 \quad P_{Gi} \geq P_{Li} \\ \quad \& Q_{Gi} \geq Q_{Li} \\ \quad \& V_{\min i} \leq V_i \leq V_{\max i} \\ 0 \quad otherwise \end{array} \right\} \quad (4)$$

Where G_i shows the total generation and L_i is the total active and reactive power consumption in state i , V_i shows the all micro grid buses in state i . after the index calculation for each state, using the each state probability, they can sum as below:

$$\rho_{\mu G} = \sum_{i=1}^N \rho_{\mu Gi} \times \rho_i \quad (5)$$

Where ρ_i is the state probability. Calculated index in equation 5 is just for a micro grid. For a system with many micro grids the success index obtained by equation 6.

$$F_2 = \frac{\sum_{k=1}^{NoM} \rho_{\mu} G_k \times N_{Lk}}{\sum_{k=1}^{NoM} N_{Lk}} \quad (6)$$

Where NoM and N_{Lk} are the number of micro grids and amount of micro grid load respectively.

C. Compound Objective Function

Two objective function can be compounded and generate an optimization objective problem:

$$\min(F), \quad F = K_1 F_1 + K_2 (1 - F_2) \quad (7)$$

It should be considered that F_1 and F_2 should be unit and F_2 modified to $1 - F_2$. K_1 and K_2 determine that objective function can be annual energy losses, success index of a micro grid or a compound of them.

Constraints of problem

Constraints of problem contains the below cases:

1) load part equations

$$P_{Sub_t} + \sum P_{DG_t} \pm \sum P_{DESR_t} - \sum P_{Load_t} \quad (8)$$

$$= \sum_{i=1}^{nbus} V_{t,i} \times V_{t,j} \times Y_{i,j} \times \cos(\theta_{ij} + \delta_{t,j} - \delta_{t,i}) \quad \forall j, t$$

$$Q_{Sub_t} + \sum Q_{DG_t} \pm \sum Q_{DESR_t} - \sum Q_{Load_t} \quad (9)$$

$$= -\sum_{i=1}^{nbus} V_{t,i} \times V_{t,j} \times Y_{i,j} \times \sin(\theta_{ij} + \delta_{t,j} - \delta_{t,i}) \quad \forall j, t$$

2) Voltage limitations

$$V_{\min} \leq V_{t,i} \leq V_{\max} \quad \forall i \neq 1 \quad (10)$$

3) Feeders capacitance limitations

$$P_{sub_t} \leq P_{rated} \quad (11)$$

4) discrete values

$$Q_{DRS_i} = k_{Q_i} \times Q_{Step} \quad \forall i \quad (12)$$

5) Penetration amount of DRS in each Bus

$$Q_{DRSs_i} \leq Q_{\max} \quad \forall i \quad (13)$$

6) Total reactive power capacity (Q_{DRS})

$$\sum_i Q_{DRSs_i} = Q_{DRS} \quad (14)$$

Problem solution algorithm

Taboo search TS (Guerrero et al. 2011 and Nunna ; Doolla 2013) is an algorithm based on iteration that uses different memory structures for the optimization problem solving. Optimization solution is vector. Its row consists of considered buses for DRS installation as below:

$$Q_{DRS} = [Q_{DRS_1} \dots Q_{DRS_k} \dots Q_{DRS_{N_c}}] \quad (15)$$

TS starts by an experimental solution and follows towards the neighborhood space. Test solution is a vector similar to Q_{DRS} , which consists of DRS measurement in each system bus. Changing the parameters of this vector, a set of vectors generated called neighborhood. Solve procedure is as below considering the K_1 and K_2 amounts.

- 1) If $K_1 \neq 0$, F_1 should calculated in connected mode to the network.
- 2) If $K_2 \neq 0$, F_2 calculated for system in islanding state, then the success index calculated via the 4 to 6 equations.

Calculating the F_1 and F_2 , objective function F , calculated for all test solutions in neighborhood and then the search process keep going until the finding best neighborhood.

Implementation and Sensitivity Analysis Studies

PG&E 69 bus distribution system used for the algorithm implementation and sensitivity analysis (Tenti et al. 2012). Active and reactive modified power shown in figure 1. In general state the energy losses is equal to 199.56 MWh. The optimum location and named capacity of DGs presented in table 1.

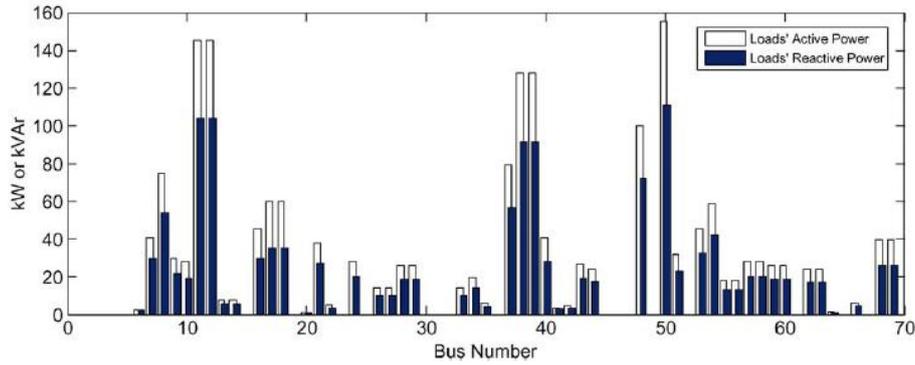


Fig1. The 69 Bus Distribution System Loads

Table1. Optimum selected Buses for the DGs installation

DG Type	Busses	Nominal Capacity(kW)
Wind Turbine	52 ,43 ,35 ,19 ,16 ,13	50 ,50 ,50 ,25 ,25 ,50
PVModule	62 ,58 ,56 ,50 ,36 ,30	25 ,25 ,25 ,25 ,25 ,25
Production of biomass dispersed	,42 ,38 ,33 ,27 ,21 ,15 ,6 68 ,57 ,54 ,45	,75 ,50 ,50 ,50 ,75 ,50 ,25 ,50 ,25 75 ,75

Table2. Micro grids with optimized design

Microgrid	Microgrid Busses	(kVA) Peak Times	Production (kVA)
	39 ,38 ,37 ,36 ,35 ,34 ,33 ,32 ,31 ,30 ,29 ,28 ,4 ,3 ,2 ,1	427/0+j304/6	225/0+j41/1
	44 ,43 ,41 ,42 ,40 ,9 ,8 ,7 ,6 ,5	246/6+j178/9	125/0+j24/7
	58 ,57 ,56 ,55 ,15 ,14 ,13 ,12 ,11 ,10	426/0+j304	225/0+j41/1
	27 ,26 ,25 ,24 ,23 ,22 ,21 ,20 ,19 ,18 ,17 ,16	265/8+j171/1	125/0+j24/6
	54 ,53 ,52 ,51 ,50 ,48 ,49 ,47 ,46 ,45	391/9+j280/4	200/0+j41/1
	69 ,68 ,67 ,66 ,65 ,64 ,63 ,62 ,61 ,60 ,59	185/6+j129/0	100/0+j24/6

Adding the DGs to the system, the energy losses reduced to 90.58MWh. Then system is divided into six virtual micro grid to minimize the active and reactive power unbalance (Chaouachi et al. 2013).Table 2 shows these six micro grids and their related properties. Figure 2 shows the system mono linear diagram. Considering the annual energy losses and success index as the objective function, the DRSs located in system as optimized form.

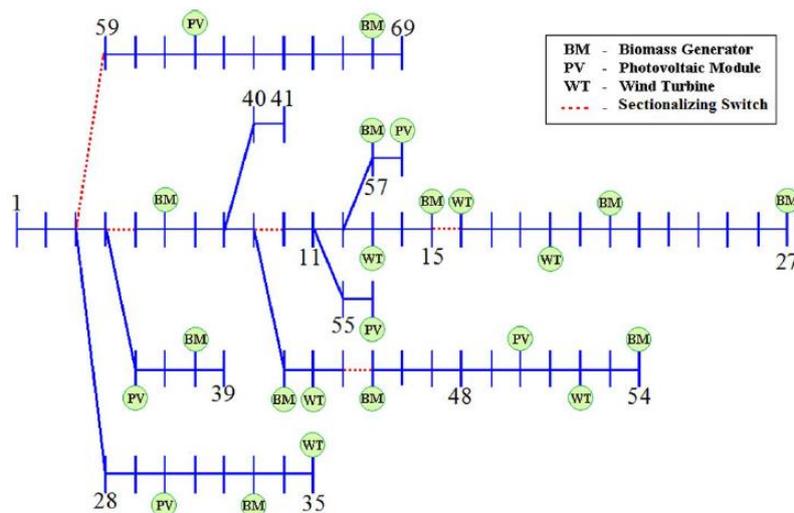


Fig2. The 69 Bus distribution system with location of distributed generations

Tabl3. DRS, their locations and capacities in stat A.

Total Capacity (kVAr)	Basses DRS	Nominal Capacity(kVAr)	Annual losses of (MWh)energy
100	53 24 3	50 22 25	78/93
150	53 52 51 24 18 3	25 25 25 25 25 25	72/43
200	54 53 50 26 17 4	25 25 50 25 50 25	66/88
250	53 52 50 21 19 17 3	25 25 75 25 25 50 25	62/28
300	57 53 51 50 21 19 18 2	25 50 25 75 25 25 50 25	58/59
350	58 53 52 50 24 18 17 13 12 3	25 25 25 100 25 50 25 25 25 25	55/49
400	57 53 52 51 50 27 22 17 15 12 11	25 25 75 25 50 25 25 50 25 50 25	52/07
450	54 53 51 50 48 23 19 18 15 12 3 57 55	25 25 50 50 25 25 25 50 25 50 25 25 50	51/07

A. Objective function of Annual energy losses (individually)

In this part, the annual energy losses considered as the objective function only to find the optimum location of DRSs in distributed system. It assumed that total capacity determined from 100 KVAR to 450 KVAR with 25 KVAR steps as the optimized form to minimize the annual energy losses. DRSs amount and their location shown in table three. It reveals that annual energy loss decrease from 78.93 MWh to 51.07 MWh in response to DRS increasing. Figure 3 shows the DRS location in situation that total amount of DRS is equal 350 KVAR. In this state, the Buses voltages modified as P.U. [0.9651-1.0016] for all states, adding the DRSs to the system. After one year, it changed to [0.9931-1.0018] P.U.

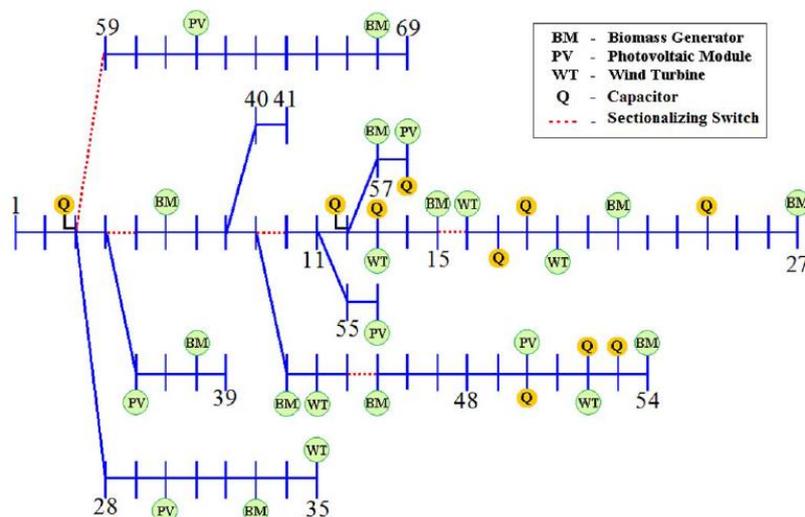


Fig3. DRSs Location in State A.

B. objective function of micro grid success index (individually)

In this part, only the success index of micro grid considered as the objective function to find the optimum location of DRSs in distribution system. In this part assumed that the total determined capacity, 100-450 KVAR, used in distribution system for optimization to success index be maximum. Table 4 shows the Success Index in the entire system in situation that DRSs located in system as optimum form. It can be seen that Success Index increases from 23.88% to 94.9%. Figure 4 the DRS location has been shown in situation that total amount of them is 350 KVAR.

Table4. DRSs, their location and capacities in situation B.

Total Capacity (kVAr)	Basses DRS	Nominal Capacity(kVAr)	Annual losses of (MWh)energy
100	61 37 33 3	25 25 25 25	23/88
150	63 33 29 27 25 2	25 25 25 25 25 25	39/47
200	67 39 38 28 27 21 3	50 25 25 25 25 25 25	54/12
250	61 59 42 38 31 28 24 17 8 4	25 25 25 25 25 25 25 25 25 25	65/98
300	51 46 41 36 31 25 21 9 3 69 63 53	25 25 25 25 25 25 25 25 25 25 25 25	71/49
350	45 44 38 33 28 26 18 8 7 3 65 63 53 48	25 25 25 25 25 25 25 25 25 25 25 25 25 25	80/79
400	39 35 33 31 23 19 15 11 7	25 25 25 25 25 25 25 25 50 25	88/11

	67 62 51 47 43	25 25 25 25 25 25 25 25 25 25	
450	31 28 27 22 15 14 11 8 7 3 64 63 58 54 51 47 43 38	25 25 25 25 25 25 25 25 25 25	94/90

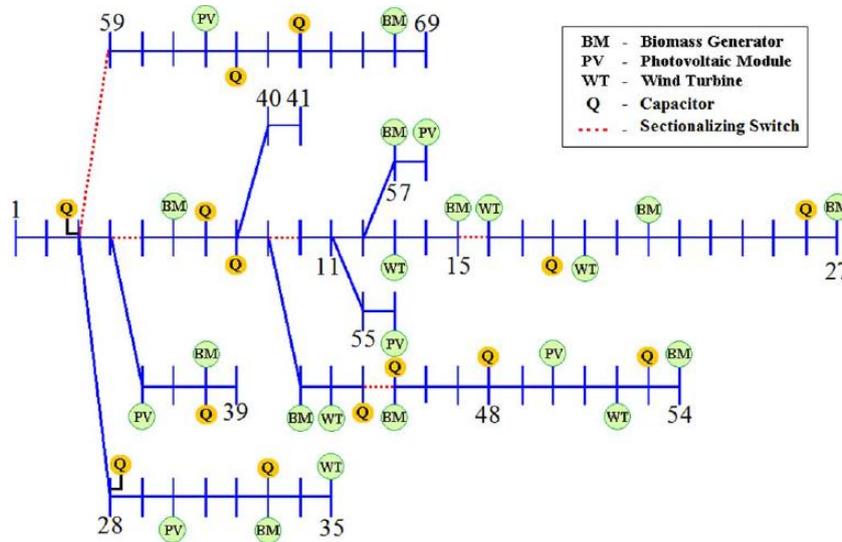


Fig4. Location of DRSs in situation B.

C. considering both objective function

In this part both objective function are considered together. For this aim, assumed that entire amount of DRSs equal to 350 KVAR. This works progressively with K_1 increasing and K_2 decreasing. The objective function in this situation will be as equation 16:

$$F = \left[\begin{array}{l} K_1 \times \left| \frac{F_1 - F_{1Opt}}{F_{1Opt}} \right| \\ + K_2 \times \left| \frac{(1 - F_2) - (1 - F_{2Opt})}{(1 - F_{2Opt})} \right| \end{array} \right] \times 100 \tag{16}$$

Table 5 shows the results of optimum locating probability of DRS in power system. Figure 5 shows the DRS location in situation that total amount of them is 350 KVAR.

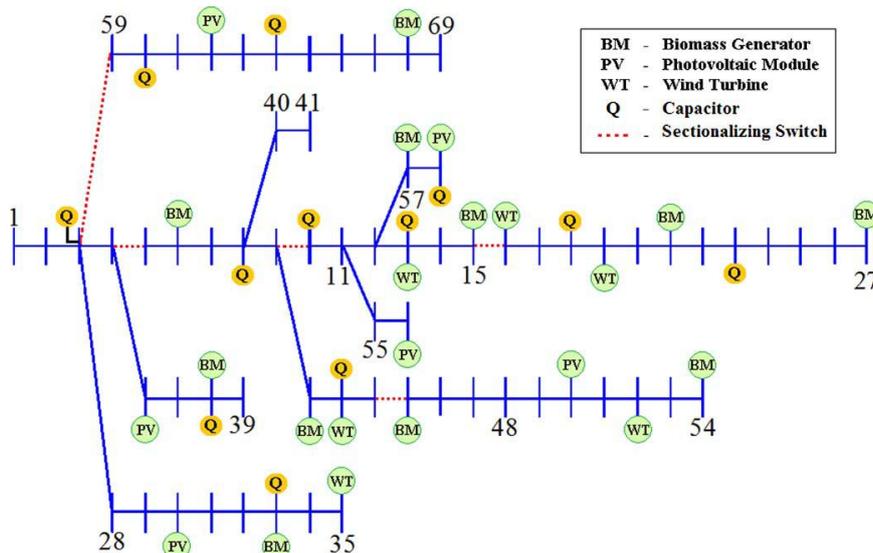


Fig5. DRSs location, considering the both objective function

Table5. DRSs, their location and capacities in situation C.

k	K	Basses DRS	Nominal Capacity(kVAr)	The objective function(%)
0	1	63 53 48 45 44 38 33 28 26 18 8 7 3 65	25 25 25 25 25 25 25 25 25 25 25 25 25 25	0/0
0/1	0/9	68 60 60 53 50 44 43 38 30 28 23 3	25 25 50 25 50 25 25 25 25 50 25	0/0225
0/3	0/7	68 63 43 38 33 28 23 20 15 13 11 3	25 25 25 25 25 25 50 25 25 25 25 25	0/1076
0/4	0/6	68 63 51 50 49 44 43 36 31 28 24 21 3	25 25 25 25 25 25 25 25 25 25 25 25	0/0927
0/5	0/5	64 60 58 43 38 33 23 18 13 10 8 3	25 25 25 25 50 25 25 25 50 25 25 25	0/1582
0/6	0/4	68 61 43 42 39 37 28 20 18 15 14 11 3	25 25 25 25 25 25 25 25 50 25 25 25	0/1761
0/7	0/3	68 63 54 51 43 38 24 23 7 3	25 25 25 75 25 50 25 50 25 25	0/1502
0/9	0/1	57 53 52 50 47 43 42 23 19 14 13 12 3 60	25 25 25 25 25 25 25 25 25 25 25 25 25	0/1495
1	0	58 53 52 50 24 18 17 13 12 3	25 25 25 100 25 50 25 25 25 25	0/0

II. Conclusion

In this article, a systematic and optimized strategy presented for DRSs optimum locating in micro grids. The TS optimization algorithm, considering the two objective function, has solved the problem. The first one is the annual energy loss and second one is the success index based on active and reactive power quality in addition to voltage limitations. In this article, assessing the some case studies, it has been shown that DRS location and amount have the significant effect on micro grid successful operation. Therefore, this problem should be reviewed for temporary part time distributed generation units.

References:

- [1]. Chaouachi, Aymen, Rashad M Kamel, Ridha Andoulsi, and Ken Nagasaka. 2013. 'Multiobjective intelligent energy management for a microgrid', IEEE Transactions on Industrial Electronics, 60: 1688-99.
- [2]. Dadkhah, Maryam, and Bala Venkatesh. 2012. 'Cumulant based stochastic reactive power planning method for distribution systems with wind generators', IEEE Transactions on Power Systems, 27: 2351-59.
- [3]. Etemadi, AH, and M Fotuhi-Firuzabad. 2008. 'Distribution system reliability enhancement using optimal capacitor placement', IET generation, transmission & distribution, 2: 621-31.
- [4]. Guerrero, Josep M, Juan C Vasquez, José Matas, Luis García De Vicuña, and Miguel Castilla. 2011. 'Hierarchical control of droop-controlled AC and DC microgrids—A general approach toward standardization', IEEE Transactions on Industrial Electronics, 58: 158-72.
- [5]. Jain, Naveen, SN Singh, and SC Srivastava. 2013. 'A generalized approach for DG planning and viability analysis under market scenario', IEEE Transactions on Industrial Electronics, 60: 5075-85.
- [6]. Mekhamer, SF, ME El-Hawary, SA Soliman, MA Moustafa, and MM Mansour. 2002. 'New heuristic strategies for reactive power compensation of radial distribution feeders', IEEE Transactions on Power Delivery, 17: 1128-35.
- [7]. Nunna, HVS Kumar, and Suryanarayana Doolla. 2013. 'Multiagent-based distributed-energy-resource management for intelligent microgrids', IEEE Transactions on Industrial Electronics, 60: 1678-87.
- [8]. Pilo, Fabrizio, Giuditta Pisano, and Gian Giuseppe Soma. 2011. 'Optimal coordination of energy resources with a two-stage online active management', IEEE Transactions on Industrial Electronics, 58: 4526-37.
- [9]. Tenti, Paolo, Alessandro Costabeber, Paolo Mattavelli, and Daniela Trombetti. 2012. 'Distribution loss minimization by token ring control of power electronic interfaces in residential microgrids', IEEE Transactions on Industrial Electronics, 59: 3817-26.